

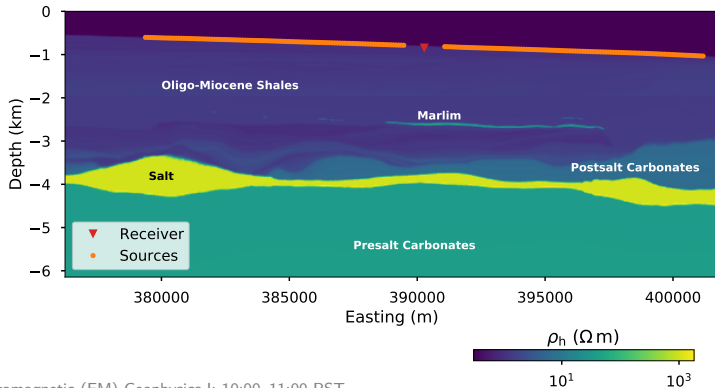
# Open-Source Landscape for Three-Dimensional Controlled-Source Electromagnetic Modeling

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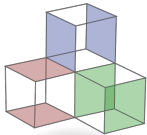
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# Validation of large-scale 3D CSEM modelling using the open-source codes `custEM`, `emg3d`, `PETGEM`, and `SimPEG`



[empymod.github.io](https://empymod.github.io)



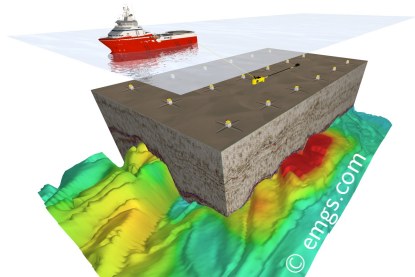
[simpeg.xyz](https://simpeg.xyz)



[petgem.bsc.es](https://petgem.bsc.es)



[custem.rtf.d.io](https://custem.rtf.d.io)

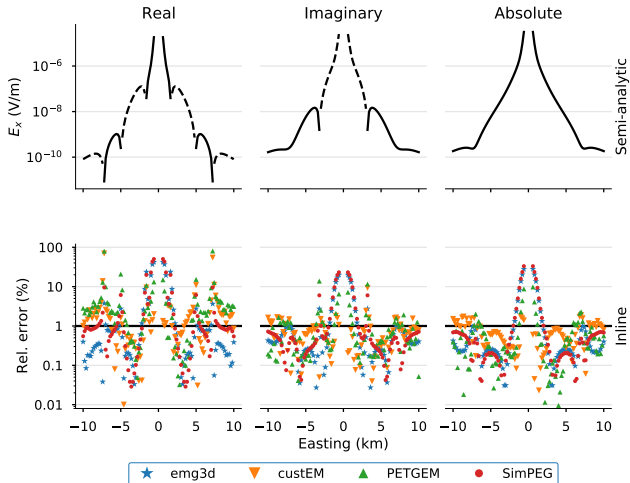
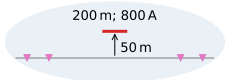
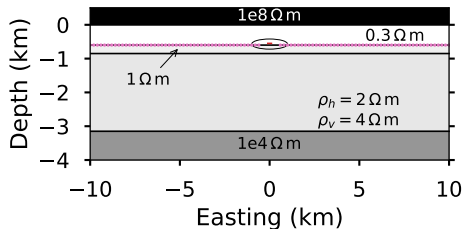


Werthmüller, Rochlitz, Castillo-Reyes, and Heagy, 2020, submitted to GJI; arXiv: 2010.12926

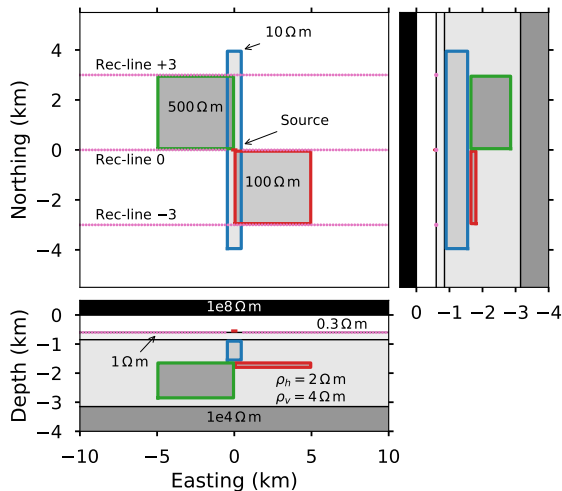
## Numerical Results

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# Verification for layered model using semi-analytical solutions shows a relative amplitude error in the order of 1 % or less



## Adding three resistive blocks to the layered model requires the normalised difference instead of the relative error

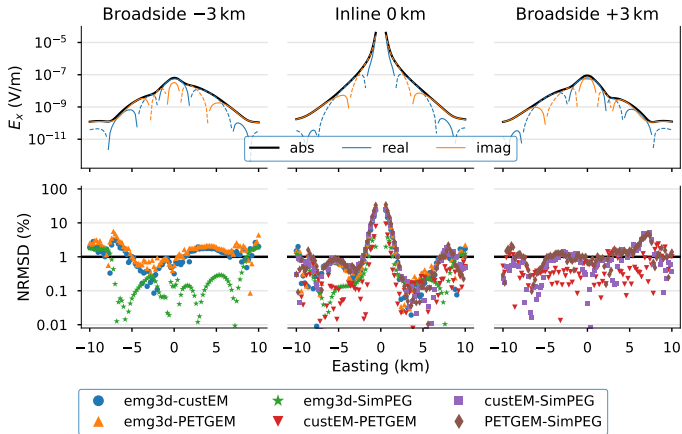
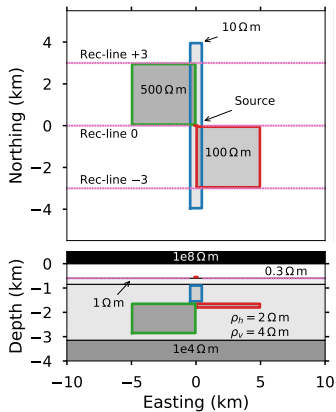


Normalised Root-Mean Square Difference (NRMSD) in percent:

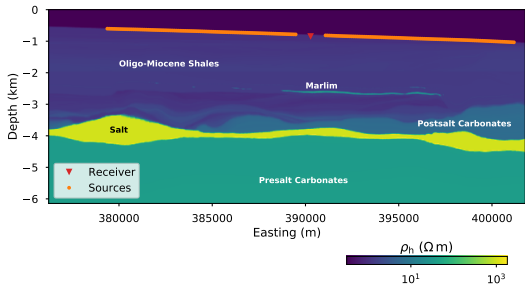
$$200 \frac{|R_1 - R_2|}{|R_1| + |R_2|}$$

After *Dublin Test Model 1*,  
Miensopust et al., 2013, GJI

# Validation between the codes shows a normalised difference of 1–2 % or less

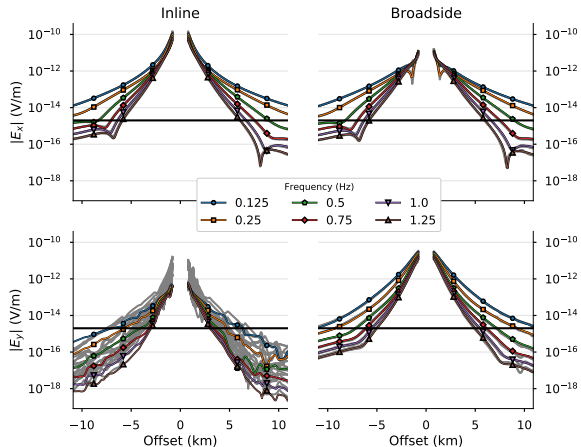


# Marlim R3D model: Responses at receiver locations look visually the same for all relevant responses

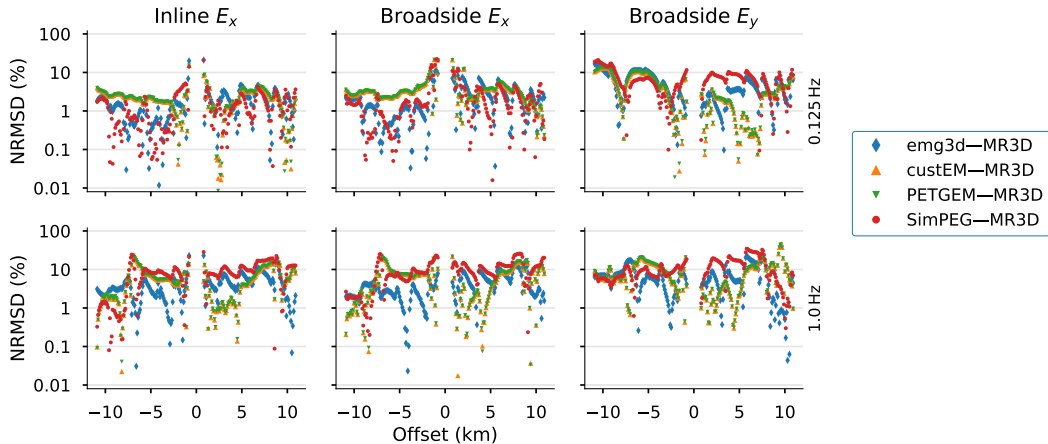


Marlim R3D:

Correa and Menezes, 2019, Geophysics

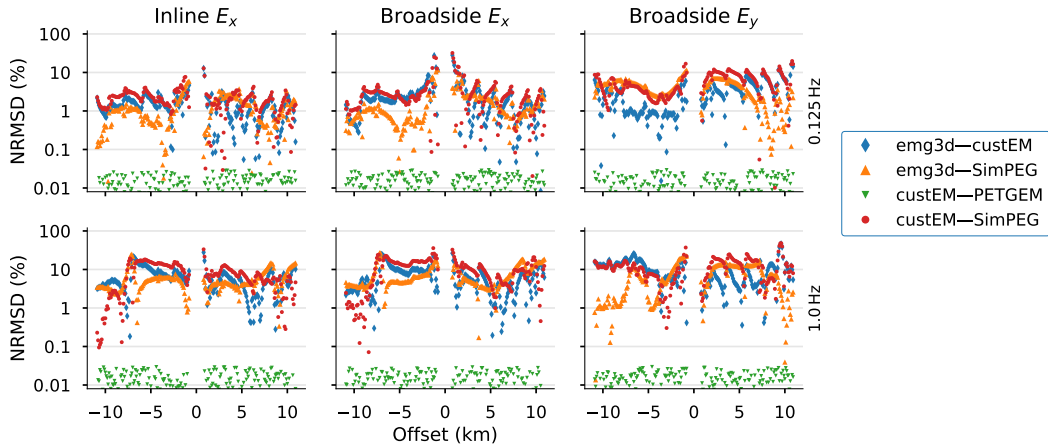


# Normalised difference to published data is mostly below 10% and very different from code to code

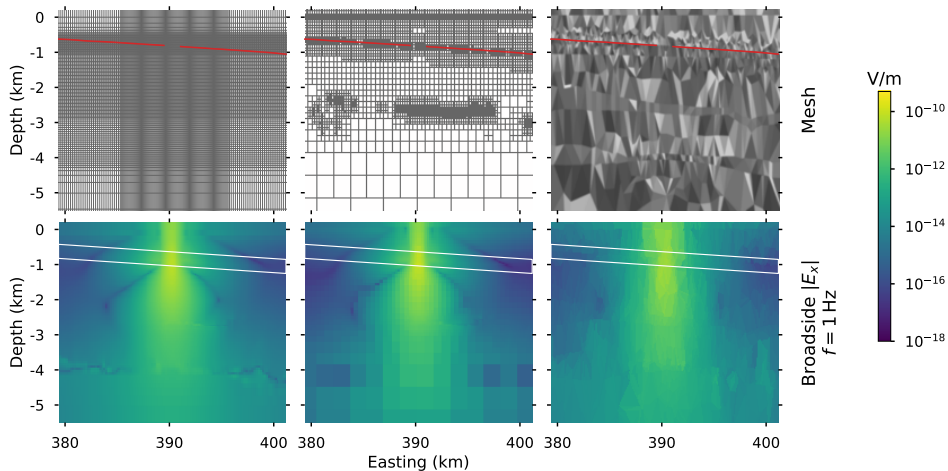




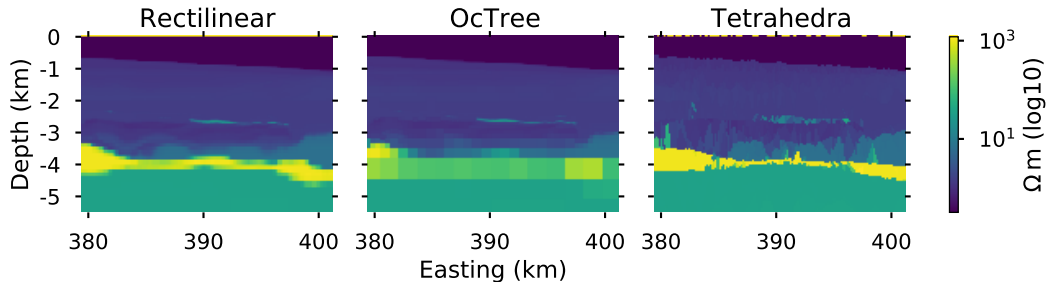
# Normalised difference between our codes is very similar and mostly below 10 %



## Very insightful is to look at the entire meshes and their different behaviours



## A look at the models in different mesh yields interesting insights with regards to recoverability in inversions



Code	#Procs	CPU (s)	RAM (GiB)	#dof
custEM	64	872	230.1	1 918 106
emg3d	1	1254	0.6	5 998 992
PETGEM	96	524	175.4	1 918 106
SimPEG	4	422	12.8	720 146

## Conclusions and Outlook

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# References

A more extensive reference list can be found in:

**Werthmüller, D., R. Rochlitz, O. Castillo-Reyes, and L. Heagy, 2020,** **Open-source landscape for 3D CSEM modelling,** submitted to *Geophysical Journal International*, arXiv: 2010.12926.

**Modelling codes:** custEM, emg3d, PETGEM, SimPEG, and empymod:

**Castillo-Reyes et al., 2018,** **PETGEM: A parallel code for 3D CSEM forward modeling using edge finite elements,** *Computers & Geosciences*, 119, 126–136, doi: 10.1016/j.cageo.2018.07.005.

**Cockett et al., 2015,** **SimPEG: An open source framework for simulation and gradient based parameter estimation in geophysical applications,** *Computers & Geosciences*, 85, 142–154, doi: 10.1016/j.cageo.2015.09.015.

**Rochlitz et al., 2019,** **custEM: customizable finite element simulation of complex controlled-source electromagnetic data,** *Geophysics*, 84, F17–F33, doi: 10.1190/geo2018-0208.1.

**Werthmüller, 2017,** **An open-source full 3D electromagnetic modeler for 1D VTI media in Python: empymod,** *Geophysics*, 82(6), WB9–WB19; doi: 10.1190/geo2016-0626.1.

**Werthmüller et al., 2019,** **emg3d: A multigrid solver for 3D electromagnetic diffusion,** *Journal of Open Source Software*, 4(39), 1463; doi: 10.21105/joss.01463.

**Solvers PETSc, MUPMS, FEniCS, and PARDISO:**

**Abhyankar et al., 2018,** **PETSc/TS: A modern scalable ODE/DAE solver library,** arXiv: 1806.01437.

**Amestoy et al., 2001,** **A fully asynchronous multifrontal solver using distributed dynamic scheduling:** *SIAM Journal on Matrix Analysis and Applications*, 23, 15–41, doi: 10.1137/S0895479899358194.

**Langtangen et al., 2016,** **Solving PDEs in Python: The FEniCS Tutorial I,** vol. 3 of *Simula SpringerBriefs on Computing*, Springer International Publishing, doi: 10.1007/978-3-319-52462-7.

**Schenk and Gärtner, 2004,** **Solving unsymmetric sparse systems of linear equations with PARDISO,** *Future Generation Computer Systems*, 20, 475–487, doi: 10.1016/j.future.2003.07.011.

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**Correa and Menezes, 2019,** **Marlim R3D: A realistic model for controlled-source electromagnetic simulations—Phase 2: The controlled-source electromagnetic data set,** *Geophysics*, 84, E293–E299, doi: 10.1190/geo2018-0452.1.

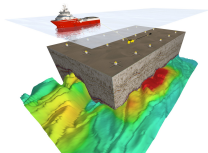
**MT comparison study:**

**Miensopust et al., 2013,** **Magnetotelluric 3-D inversion—a review of two successful workshops on forward and inversion code testing and comparison,** *Geophysical Journal International*, 193, 1216–1238, doi: 10.1093/gji/ggt066.

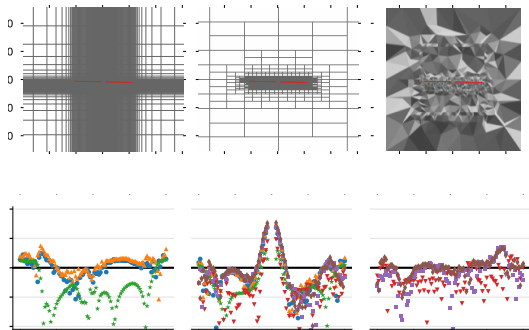
# More Comparisons & Benchmarks

## Other Scenarios, other programming languages

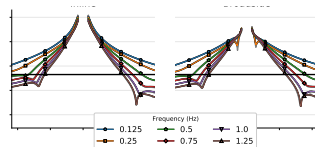
emg3d



custEM



simpeg



getgem